# Piezoelectric Energy Harvester 

## Introduction

The development of extremely low power electronics and wireless systems has led to a strong interest in the field of energy harvesting - the development of miniature generators. Typically these devices are used to power sensors and wireless communication systems, enabling standalone 'wireless sensors' that are cheap to deploy. Frequently wireless sensors make measurements intermittently over an extended period, reporting via a wireless link to other sensors and ultimately to a base station that records readings from all the deployed sensors (creating a 'wireless sensor network'). This model analyzes a simple "seismic" energy harvester, that is designed to generate electrical energy from local variations in acceleration, that occur, for example, when a wireless sensor is mounted on a vibrating piece of machinery. The energy harvester analyzed in this model consists of a piezoelectric bimorph clamped at one end to the vibrating machinery with a proof mass mounted on its other end. It is loosely based on the mechanical system described in detail in Ref. 1.

## Model Definition

Figure 1 shows the device geometry. The power harvester consists of a piezoelectric bimorph clamped at one end with a proof mass mounted on the other end. The bimorph has a ground electrode embedded within it (coincident with the neutral plane of the beam) and two electrodes on the exterior surfaces of the cantilever beam. This configuration ensures that same voltage is induced on the exterior electrodes, even though the stress above and below the neutral layer is of opposite sign. Since the clamp is mounted to a piece of vibrating machinery the device is analyzed in a vibrating reference frame (modeled in COMSOL by the application of a sinusoidal body load).


Figure 1: 2D model geometry, showing the major components of the energy harvester, including the piezoelectric bimorph, proof mass and supporting structure.

The model performs three analyses of the mechanical part of the energy harvester system. First, the power output is analyzed as a function of vibration frequency, with a fixed electrical load. Then the power output as a function of electrical load is explored. Finally the DC voltage output, as a function of acceleration, is shown to be linear.

## Results and Discussion

Figure 2 shows the input mechanical power and the power harvested (in mW ) as well as the peak voltage induced across the piezoelectric bimorph (in V ) as a function of frequency when the energy harvester is excited by a sinusoidal acceleration. The electrical load is $12 \mathrm{k} \Omega$. The response of the system shows a peak at 76 Hz , close to the computed resonant frequency of the cantilever at 73 Hz (from a separate eigenfrequency analysis of this device).


Figure 2: Energy barvester input mechanical power and the power harvested (in $m W$ ) as well as the peak voltage induced across the piezoelectric bimorph (in V) ps. excitation frequency. The load impedance is $12 \mathrm{k} \Omega$ and the acceleration magnitude is 1 g .


Figure 3: Power harvested from the device as a function of the electrical load resistance at an acceleration of $1 \mathscr{g}$ oscillating at 75.5 Hz .

Figure 3 shows the harvested power from the device as a function of the electrical load resistance at an acceleration of 1 g oscillating at 75.5 Hz . The peak in energy harvested corresponds to an electrical load of $6 \mathrm{k} \Omega$.


Figure 4: DC voltage and mechanical/electrical power output versus the magnitude of the mechanical acceleration at a fixed frequency of 75.5 Hz with a load impedance of $12 \mathrm{k} \Omega$.

Figure 4 shows the DC voltage and mechanical/electrical power output versus the magnitude of the mechanical acceleration at a fixed frequency of 75.5 Hz with a load impedance of $12 \mathrm{k} \Omega$. The voltage increases linearly with the load, whilst the harvested power increases quadratically, as expected from equation 4 in Ref. 1 .

Note that these results are in good qualitative agreement with those presented in Ref. 1. Completely quantitative agreement would not be expected from a two dimensional model.

## References

1. E. Lefeuvre, D. Audiger, C. Richard and D. Guyomar, "Buck-Boost Converter for Sensorless Power Optimization of Piezoelectric Energy Harvester", IEEE
Transactions on Power Electronics, vol. 22, no. 5, 2007.
```
Application Library path: MEMS_Module/Piezoelectric_Devices/
piezoelectric_energy_harvester
```


## Modeling Instructions

From the File menu, choose New.

## NE W

I In the New window, click Model Wizard.

## MODEL WIZARD

I In the Model Wizard window, click 2D.
2 In the Select physics tree, select Structural Mechanics>Piezoelectric Devices.
3 Click Add.
4 In the Select physics tree, select AC/DC>Electrical Circuit (cir).
5 Click Add.
6 Click Study.
7 In the Select study tree, select Preset Studies for Selected Physics Interfaces>Frequency Domain.

8 Click Done.

## GLOBAL DEFINITIONS

## Parameters

I On the Home toolbar, click Parameters.
2 In the Settings window for Parameters, locate the Parameters section.
3 In the table, enter the following settings:

| Name | Expression | Value | Description |
| :--- | :--- | :--- | :--- |
| acc | 1 | l | Acceleration (g) |
| R_load | $12[\mathrm{kohm}]$ | $12000 \Omega$ | Load resistance |
| w_plate | $14[\mathrm{~mm}]$ | 0.014 m | Out of plane dimension |

## GEOMETRY I

I In the Model Builder window, under Component I (compl) click Geometry I.
2 In the Settings window for Geometry, locate the Units section.
3 From the Length unit list, choose mm.
Rectangle I (rl)
I On the Geometry toolbar, click Primitives and choose Rectangle.
2 In the Settings window for Rectangle, locate the Position section.
3 In the $\mathbf{x}$ text field, type-1.
4 In the $y$ text field, type - 1 .
Rectangle 2 (r2)
I On the Geometry toolbar, click Primitives and choose Rectangle.
2 In the Settings window for Rectangle, locate the Size and Shape section.
3 In the Width text field, type 21.
4 In the Height text field, type 0.16.
5 Locate the Position section. In the $\mathbf{x}$ text field, type -1.
6 Click to expand the Layers section. In the table, enter the following settings:

| Layer name | Thickness (mm) |
| :--- | :--- |
| Layer 1 | 0.06 |
| Layer 2 | 0.04 |

## Rectangle 3 (r3)

I On the Geometry toolbar, click Primitives and choose Rectangle.
2 In the Settings window for Rectangle, locate the Size and Shape section.
3 In the Width text field, type 4.
4 In the Height text field, type 1.7.
5 Locate the Position section. In the $\mathbf{x}$ text field, type 16 .
6 In the $y$ text field, type 0.16.
Union I (unil)
I On the Geometry toolbar, click Booleans and Partitions and choose Union.
2 Select the objects $\mathbf{r I}$ and $\mathbf{r 2}$ only.
3 In the Settings window for Union, locate the Union section.
4 Under Input_objects, click Zoom to Selection.

5 Click in the Graphics window and then press Ctrl+A to select all objects.
6 Clear the Keep interior boundaries check box.
Add chamfers to the model to avoid stress singularities at the reentrant corners.

## Chamfer I (chal)

I On the Geometry toolbar, click Chamfer.
2 On the object unil, select Points 7 and 8 only.
3 In the Settings window for Chamfer, locate the Distance section.
4 In the Distance from vertex text field, type 0.25.
Rectangle 2 (r2)
In the Model Builder window, under Component I (compl)>Geometry I right-click Rectangle 2 (r2) and choose Duplicate.

## Bézier Polygon I (bl)

I On the Geometry toolbar, click Primitives and choose Bézier Polygon.
2 In the Settings window for Bézier Polygon, locate the Polygon Segments section.
3 Find the Added segments subsection. Click Add Linear.
4 Find the Control points subsection. In row $\mathbf{I}$, set $\mathbf{x}$ to 0.25 .
5 In row 2 , set $\mathbf{x}$ to 0.25 .
6 In row 2 , set $y$ to 0.16 .
Bézier Polygon 2 (b2)
I On the Geometry toolbar, click Primitives and choose Bézier Polygon.
2 In the Settings window for Bézier Polygon, locate the Polygon Segments section.
3 Find the Added segments subsection. Click Add Linear.
4 Find the Control points subsection. In row $\mathbf{I}$, set $\mathbf{x}$ to 15.75 .
5 In row $\mathbf{2}$, set $\mathbf{x}$ to 15.75 .
6 In row I , set $\mathbf{y}$ to 0.16 .
7 On the Geometry toolbar, click Build All.

## MATERIALS

On the Home toolbar, click Windows and choose Add Material.

## ADD MATERIAL

I Go to the Add Material window.

2 In the tree, select Piezoelectric>Lead Zirconate Titanate (PZT-5A).
3 Click Add to Component in the window toolbar.

## ADD MATERIAL

I Go to the Add Material window.
2 In the tree, select Built-In>Structural steel.
3 Click Add to Component in the window toolbar.
4 On the Home toolbar, click Add Material to close the Add Material window.

## MATERIALS

## Structural steel (mat2)

I In the Model Builder window, under Component I (compl)>Materials click Structural steel (mat2).

2 Select Domains 1, 3, 6, 9, and 11 only.

SOLID MECHANICS (SOLID)

## Linear Elastic Material I

In the Model Builder window, under Component I (comp I) $>$ Solid Mechanics (solid) click Linear Elastic Material I.

Damping I
I On the Physics toolbar, click Attributes and choose Mechanical Damping.
2 In the Settings window for Damping, locate the Damping Settings section.
3 From the Damping type list, choose Isotropic loss factor.
4 From the $\eta_{\mathrm{s}}$ list, choose User defined. In the associated text field, type 0.001 .

## Piezoelectric Material I

I In the Model Builder window, under Component I (compl)>Solid Mechanics (solid) click Piezoelectric Material I.
2 In the Settings window for Piezoelectric Material, locate the Domain Selection section.

3 From the Selection list, choose Manual.
4 Select Domains 2, 4, 5, 7, 8, and 10 only.
Mechanical Damping I
I On the Physics toolbar, click Attributes and choose Mechanical Damping.

2 In the Settings window for Mechanical Damping, locate the Damping Settings section.

3 From the Damping type list, choose Isotropic loss factor.
4 From the $\eta_{\mathrm{S}}$ list, choose User defined. In the associated text field, type 0.001 .
Body Load I
I On the Physics toolbar, click Domains and choose Body Load.
2 In the Settings window for Body Load, locate the Domain Selection section.
3 From the Selection list, choose All domains.
4 Locate the Force section. Specify the $\mathbf{F}_{\mathrm{V}}$ vector as

| 0 | $x$ |
| :--- | :--- |
| -solid.rho*g_const*acc | $y$ |

## Fixed Constraint I

I On the Physics toolbar, click Boundaries and choose Fixed Constraint.
2 Select Boundary 2 only.

## ELECTROSTATICS (ES)

I In the Model Builder window, under Component I (compl) click Electrostatics (es).
2 Select Domains 2, 4, 5, 7, 8, and 10 only.
3 In the Settings window for Electrostatics, locate the Thickness section.
4 In the $d$ text field, type w_plate.

## Ground I

I On the Physics toolbar, click Boundaries and choose Ground.
2 Select Boundaries $4,9,13,18,20$, and 26 only.

## Terminal I

I On the Physics toolbar, click Boundaries and choose Terminal.
2 Select Boundaries $6,8,15,17,22$, and 24 only.
3 In the Settings window for Terminal, locate the Terminal section.
4 From the Terminal type list, choose Circuit.

ELECTRICAL CIRCUIT (CIR)
In the Model Builder window, under Component I (compl) click Electrical Circuit (cir).

## Resistor I

I On the Electrical Circuit toolbar, click Resistor.
2 In the Settings window for Resistor, locate the Node Connections section.
3 In the table, enter the following settings:

| Label | Node names |
| :--- | :--- |
| n | 0 |

4 Locate the Device Parameters section. In the $R$ text field, type R_load.

## External I-Terminal I

I On the Electrical Circuit toolbar, click External I-Terminal.
2 In the Settings window for External I-Terminal, locate the Node Connections section.
3 In the Node name text field, type 1.
4 Locate the External Terminal section. From the $V$ list, choose Terminal voltage (es/ terml).

## MESH I

I In the Model Builder window, under Component I (compl) click Mesh I.
2 In the Settings window for Mesh, locate the Mesh Settings section.
3 From the Sequence type list, choose User-controlled mesh.

## Mapped I

I Right-click Component I (compI)>Mesh I and choose Mapped.
2 In the Settings window for Mapped, locate the Domain Selection section.
3 From the Geometric entity level list, choose Domain.
4 Select Domains 5-7 only.
Distribution I
I Right-click Component I (compI)>Mesh I>Mapped I and choose Distribution.
2 Select Boundaries 19 and 23 only.
3 In the Settings window for Distribution, locate the Distribution section.
4 In the Number of elements text field, type 3.

## Distribution 2

I Right-click Mapped I and choose Distribution.
2 Select Boundary 21 only.

3 In the Settings window for Distribution, locate the Distribution section.
4 In the Number of elements text field, type 2.

## Distribution 3

I Right-click Mapped I and choose Distribution.
2 Select Boundaries 13, 15, 17, and 18 only.
3 In the Settings window for Distribution, locate the Distribution section.
4 From the Distribution properties list, choose Predefined distribution type.
5 In the Number of elements text field, type 30.
6 In the Element ratio text field, type 20.
7 Select the Reverse direction check box.

## Mapped 2

I In the Model Builder window, right-click Mesh I and choose Mapped.
2 In the Settings window for Mapped, locate the Domain Selection section.
3 From the Geometric entity level list, choose Domain.
4 Select Domains 8-10 only.
Distribution I
I Right-click Component I (compl)>Mesh I>Mapped 2 and choose Distribution.
2 Select Boundaries 20, 22, 24, and 26 only.
3 In the Settings window for Distribution, locate the Distribution section.
4 From the Distribution properties list, choose Predefined distribution type.
5 In the Number of elements text field, type 10.
6 In the Element ratio text field, type 20.
7 Select the Reverse direction check box.

## Mapped 3

I In the Model Builder window, right-click Mesh I and choose Mapped.
2 In the Settings window for Mapped, locate the Domain Selection section.
3 From the Geometric entity level list, choose Domain.
4 Select Domains 2-4 only.
Distribution I
I Right-click Component I (compl)>Mesh I>Mapped 3 and choose Distribution.
2 Select Boundaries 4, 6, 8, and 9 only.

3 In the Settings window for Distribution, locate the Distribution section.
4 From the Distribution properties list, choose Predefined distribution type.
5 In the Number of elements text field, type 10.
6 In the Element ratio text field, type 10.

## Free Triangular I

I In the Model Builder window, under Component I (compI)>Mesh I right-click Free Triangular I and choose Move Down.

2 Right-click Component I (compI)>Mesh I>Free Triangular I and choose Move Down.
3 Right-click Component I (compI)>Mesh I>Free Triangular I and choose Move Down.
4 On the Home toolbar, click Build Mesh.


STUDY I
I In the Model Builder window, click Study I.
2 In the Settings window for Study, type Frequency Response in the Label text field.

## FREQUENCY RESPONSE

## Step 1: Frequency Domain

I In the Model Builder window, under Frequency Response click Step I: Frequency Domain.

2 In the Settings window for Frequency Domain, locate the Study Settings section.
3 In the Frequencies text field, type 60677072 range (73, .5,78) 79818590 .
Disable direct solver error checking which is too stringent in this case.

## Solution I (soll)

I On the Study toolbar, click Show Default Solver.
2 In the Model Builder window, expand the Solution I (soll) node.

## DEFINITIONS

Define an integration operator to calculate mechanical power input later when plotting results.

## Integration I (intop I)

I On the Definitions toolbar, click Component Couplings and choose Integration.
2 In the Settings window for Integration, locate the Source Selection section.
3 From the Selection list, choose All domains.

## FREQUENCY RESPONSE

Solution I (soll)
I In the Model Builder window, under Frequency Response $>$ Solver Configurations>Solution I (solI)>Stationary Solver I click Direct.

2 In the Settings window for Direct, click to expand the Error section.
3 From the Check error estimate list, choose No.
4 On the Home toolbar, click Compute.

## RESULTS

## ID Plot Group 3

I On the Home toolbar, click Add Plot Group and choose ID Plot Group.
2 In the Settings window for 1D Plot Group, type Frequency Response: Voltage \& power in the Label text field.

3 Click to expand the Title section. From the Title type list, choose Manual.

4 In the Title text area, type Frequency Response: Voltage \& power.

## Global I

On the Frequency Response: Voltage \& power toolbar, click Global.

## Frequency Response: Voltage \& power

I In the Settings window for Global, locate the $\boldsymbol{y}$-Axis Data section.
2 In the table, enter the following settings:

| Expression | Unit | Description |
| :---: | :---: | :---: |
| abs(cir.R1_v) | V | voltage (V) |
| 0.5*intop1 (realdot(-soli <br> d.rho*g_const*acc, solid. u_tY))*w_plate | mW | mechanical power in (mW) |
| $\begin{aligned} & 0.5^{*} \text { realdot(cir.R1_i, cir } \\ & . \text { R1_v) } \end{aligned}$ | mW | electric power out (mW) |

3 Click to expand the Coloring and style section. Locate the Coloring and Style section. In the Width text field, type 2.

4 Find the Line markers subsection. From the Marker list, choose Cycle.
5 From the Positioning list, choose In data points.
6 On the Frequency Response: Voltage \& power toolbar, click Plot.

## ROOT

On the Home toolbar, click Windows and choose Add Study.

## ADD STUDY

I Go to the Add Study window.
2 Find the Studies subsection. In the Select study tree, select Preset Studies.
3 In the Select study tree, select Preset Studies>Frequency Domain.
4 Click Add Study in the window toolbar.
5 On the Home toolbar, click Add Study to close the Add Study window.

## STUDY 2

## Step I: Frequency Domain

I In the Model Builder window, under Study 2 click Step I: Frequency Domain.
2 In the Settings window for Frequency Domain, locate the Study Settings section.
3 In the Frequencies text field, type 75.5.

4 Click to expand the Study extensions section. Locate the Study Extensions section. Select the Auxiliary sweep check box.

## 5 Click Add.

6 In the table, enter the following settings:

| Parameter name | Parameter value list | Parameter unit |
| :--- | :--- | :--- |
| R_load | $10^{\wedge}$ range $(2,0.25,5)$ |  |

7 In the Model Builder window, click Study 2.
8 In the Settings window for Study, type Load dependence in the Label text field.
9 Locate the Study Settings section. Clear the Generate default plots check box.
10 On the Study toolbar, click Show Default Solver.

## LOAD DEPENDENCE

## Solution 2 (sol2)

I In the Model Builder window, expand the Solution 2 (sol2) node.
2 In the Model Builder window, expand the Load dependence $>$ Solver Configurations>Solution 2 (sol2)>Stationary Solver I node, then click Direct.

3 In the Settings window for Direct, locate the Error section.
4 From the Check error estimate list, choose No.
5 On the Study toolbar, click Compute.

## RESULTS

Frequency Response: Voltage \& power I
I In the Model Builder window, under Results right-click Frequency Response: Voltage \& power and choose Duplicate.

2 In the Settings window for 1D Plot Group, type Load dependence: Voltage \& power in the Label text field.
3 Locate the Data section. From the Data set list, choose Load dependence/Solution 2 (sol2).

## Load dependence: Voltage \& power

I Locate the Title section. In the Title text area, type Load dependence: Voltage \& power.

2 Click to expand the Legend section. From the Position list, choose Upper left.

3 Click the x-Axis Log Scale button on the Graphics toolbar.
4 On the Load dependence: Voltage \& power toolbar, click Plot.

## ROOT

On the Home toolbar, click Windows and choose Add Study.

## ADD STUDY

I Go to the Add Study window.
2 Find the Studies subsection. In the Select study tree, select Preset Studies>Frequency Domain.

3 Click Add Study in the window toolbar.
4 On the Home toolbar, click Add Study to close the Add Study window.

## STUDY 3

## Step I: Frequency Domain

I In the Model Builder window, expand the Results>Load dependence: Voltage \& power node, then click Study 3>Step I: Frequency Domain.

2 In the Settings window for Frequency Domain, locate the Study Settings section.
3 In the Frequencies text field, type 75.5.
4 Locate the Study Extensions section. Select the Auxiliary sweep check box.
5 Click Add.
6 In the table, enter the following settings:

| Parameter name | Parameter value list | Parameter unit |
| :--- | :--- | :--- |
| acc | range $(0.25,0.25,2)$ |  |

7 In the Model Builder window, click Study 3.
8 In the Settings window for Study, type Acceleration dependence in the Label text field.

9 Locate the Study Settings section. Clear the Generate default plots check box.
10 On the Study toolbar, click Show Default Solver.

## ACCELERATION DEPENDENCE

## Solution 3 (sol3)

I In the Model Builder window, expand the Solution 3 (sol3) node.

2 In the Model Builder window, expand the Acceleration dependence>Solver Configurations>Solution $\mathbf{3}$ (sol3)>Stationary Solver I node, then click Direct.

3 In the Settings window for Direct, locate the Error section.
4 From the Check error estimate list, choose No.
5 On the Study toolbar, click Compute.

## RESULTS

Load dependence: Voltage \& power I
I In the Model Builder window, under Results right-click Load dependence: Voltage \& power and choose Duplicate.

2 In the Settings window for 1D Plot Group, type Acceleration dependence: Voltage \& power in the Label text field.

3 Locate the Data section. From the Data set list, choose Acceleration dependence/ Solution 3 (sol3).

4 Locate the Plot Settings section. Select the $\mathbf{x}$-axis label check box.
5 In the associated text field, type acceleration (g).
6 Locate the Axis section. Clear the $\mathbf{x}$-axis log scale check box.
7 Locate the Title section. In the Title text area, type Acceleration dependence: Voltage \& power.

8 On the Acceleration dependence: Voltage \& power toolbar, click Plot.

